

# Origin Of $\text{CH}^+$ In Diffuse Molecular Clouds

## Outline

- ①  $\text{CH}^+$  in the diffuse ISM
- ② Hybrid approach for the chemistry
- ③ Warm  $\text{H}_2$  and ion-neutral drift
- ④ Summary

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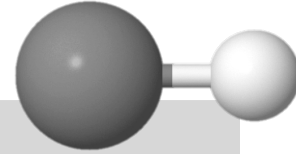
(A&A in press)



Laboratoire d'Étude du Rayonnement et de la Matière en Astrophysique

- Simple hydride
- Easily **destroyed**
- Main formation path is **highly endothermic**  

$$\text{C}^+ + \text{H}_2 \rightarrow \text{CH}^+ + \text{H} \quad (\Delta E/k = -4300 \text{ K}).$$
- Classical PDR models **predict low abundances** in the diffuse ISM
- But observations reveal **relatively high abundances**



## SPECIES DATA

Name	Methylidyne cation
Common Formula	CH <sup>+</sup>
Mass	13.00728 <i>a.m.u</i>
Charge	1
CAS	24361-82-8
Inchi	InChI=1S/CH/h1H/q+1
InchiKey	WVVLBIYUCXYEU-UHFFFAOYSA-N
Electronic State	
Excitation	Ground State

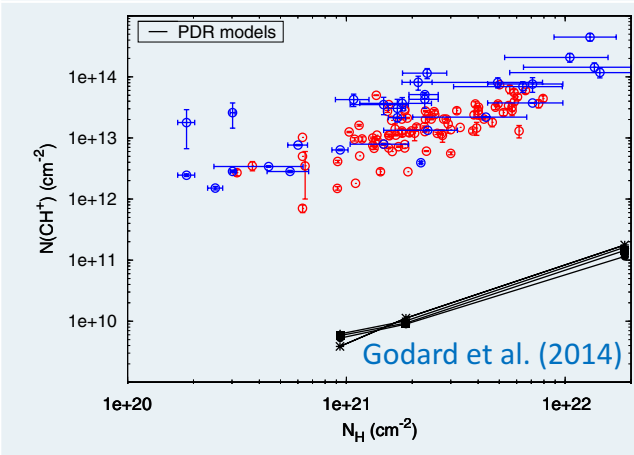
# CH<sup>+</sup> In The Diffuse ISM: Goal

Impact of the turbulent mixing CNM/WNM on the chemistry  
Impact of the multiphase structure

# CH<sup>+</sup> In The Diffuse ISM: Previous Attempts

## PDR Models

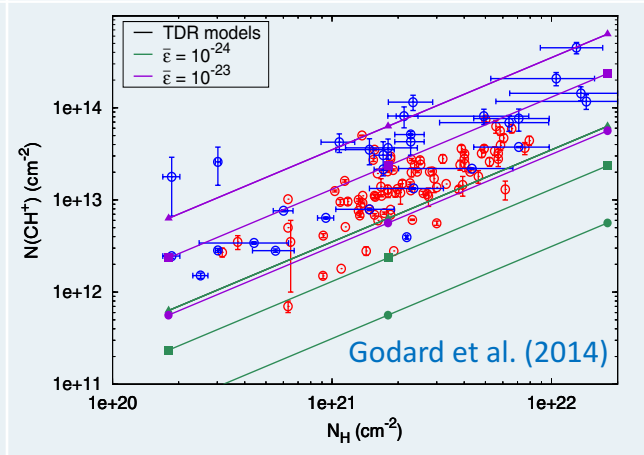
Stationary plane-parallel slabs illuminated from one or two sides



Simple geometry, it does not take into account the dynamics nor the fractal-like structure of real molecular clouds.

## Dissipation of Turbulence

Burst of dissipation  
L~10 AU ; t~100 yr



Do not consider the role of gas dynamics nor the 3D structure  
Underlying dissipation processes are imposed  
(Falgarone et al. 2010, Godard et al. 2009, 2014)

## Ion-Neutral Drift

$$T_{\text{eff}} = \frac{m_i T_n + m_n T_i}{m_i + m_n} + \Delta T,$$

$$\Delta T = \frac{\mu}{3k} v_d^2$$

$N_{\text{CH}^+}$ ( $10^{13} \text{ cm}^{-2}$ )	$N_{\text{H}}$ ( $10^{21} \text{ cm}^{-2}$ )	$\bar{v}_{d,99}$ ( $\text{km s}^{-1}$ )
1.1	2.2	2.1
0.8	2.2	3.0
1.1	1.2	2.3
0.9	1.3	2.2
0.6	1.9	1.7
1.4	2.0	2.5
1.6	1.9	2.2
1.2	2.7	1.9

Do not treat microphysics  
Constant ion density  
(Myers et al. 2015)

**Other approaches:** Alfvén waves (Federman et al. 1996), Low velocity C-shocks (Draine & Katz 1986), Irradiated low-v C-shocks (Lesaffre et al. 2013)

## On-the-fly

- Crucial species for the chemistry:  $\text{H}_2$  which is a **bottleneck** for the chemistry.

$$\frac{\partial n_{\text{H}_2}}{\partial t} + \nabla \cdot (n_{\text{H}_2} \mathbf{v}) = k_{\text{form}} n(n - 2n_{\text{H}_2}) - k_{\text{ph}} n_{\text{H}_2}$$

- Heating: PE, CR,  $\text{H}_2$  (formation and destruction)
- Use cooling functions: CII, OI,  $\text{Ly}\alpha$ , Rec,  $\text{H}_2$
- Compute dust shielding and  $\text{H}_2$  self-shielding  
 $f_{\text{sh}, \text{H}_2} = \langle e^{-\tau_{a,1000}} f_{\text{shield}} \rangle$
- Solve ideal MHD equations.

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) = 0,$$

$$\frac{\partial \rho \mathbf{v}}{\partial t} + \nabla \cdot (\rho \mathbf{v} \mathbf{v} - \mathbf{B} \mathbf{B}) + \nabla P = -\rho \nabla \phi,$$

$$\frac{\partial E}{\partial t} + \nabla \cdot [(E + P) \mathbf{v} - \mathbf{B}(\mathbf{B} \mathbf{v})] = -\rho \mathcal{L},$$

$$\frac{\partial \mathbf{B}}{\partial t} + \nabla \cdot (\mathbf{v} \mathbf{B} - \mathbf{B} \mathbf{v}) = 0,$$

$$\nabla^2 \phi = 4\pi G \rho,$$

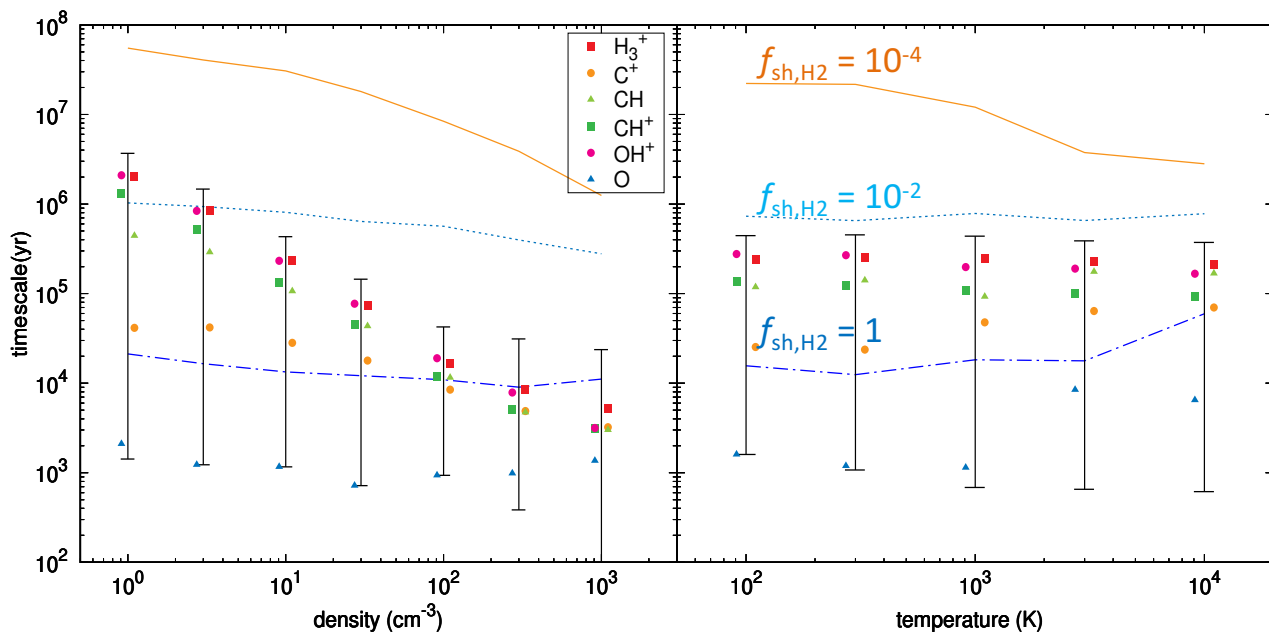
## Post-processing

- Compute the **equilibrium** abundances for all the species (besides  $\text{H}_2$  and HI)
- Compute the ion-neutral drift velocity  $v_d$
- Use local physical conditions ( $n$ ,  $T$ ,  $A_V$ ,  $f_{\text{sh}, \text{H}_2}$ )

mandatory			
$\chi$	Mathis	1	external UV radiation field
$A_V$	mag	0 – 10	visible extinction
$T_K$	K	$10 - 10^4$	kinetic temperature
$n_{\text{H}}$	$\text{cm}^{-3}$	$10^{-1} - 10^4$	gas density
$\zeta_{\text{H}_2}$	$\text{s}^{-1}$	$3 \times 10^{-16}$	CR ionisation rate of $\text{H}_2$
optional			
$f_{\text{sh}, \text{H}_2}$		$10^{-8} - 1$	$\text{H}_2$ self-shielding factor <sup>a</sup>
$f_{\text{sh}, \text{CO}}$		1	CO self-shielding factor <sup>b</sup>
$x(\text{H}_2)$		$10^{-7} - 1$	$\text{H}_2$ abundance
$v_d$	$\text{km s}^{-1}$	0 – 5	ion-neutral velocity drift

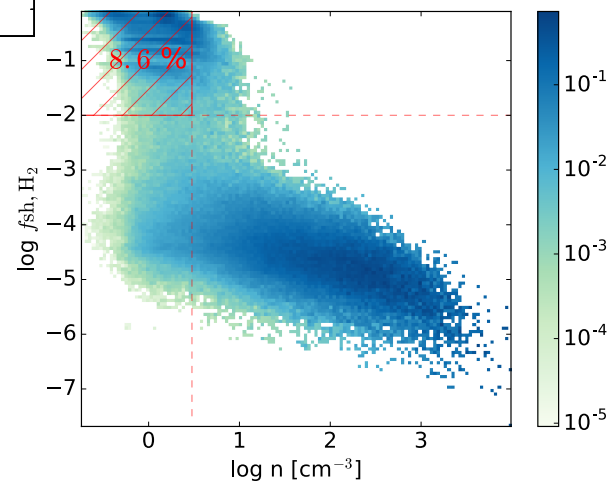
(a) Valdivia et al. (2016) (b) not computed in the simulation

# Hybrid Approach For The Chemistry: Validity



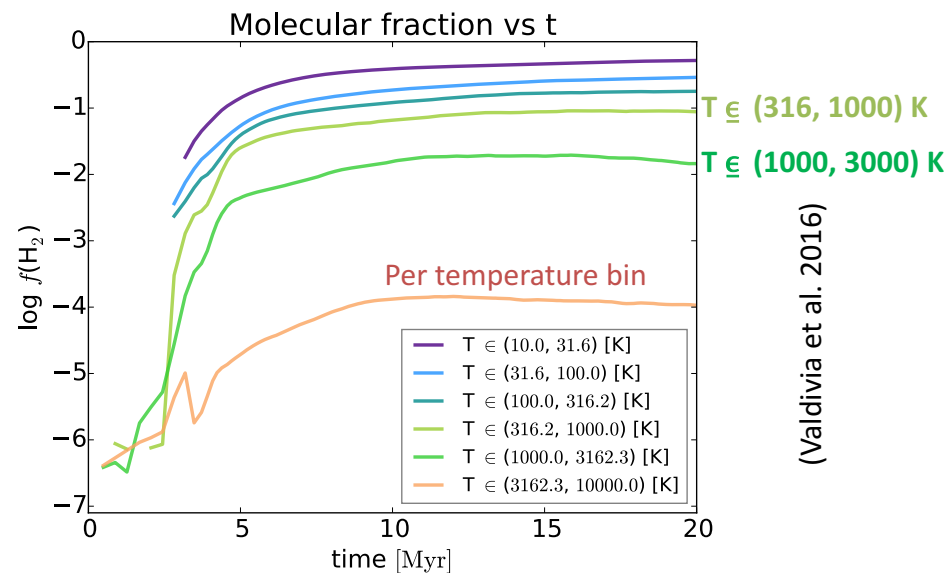
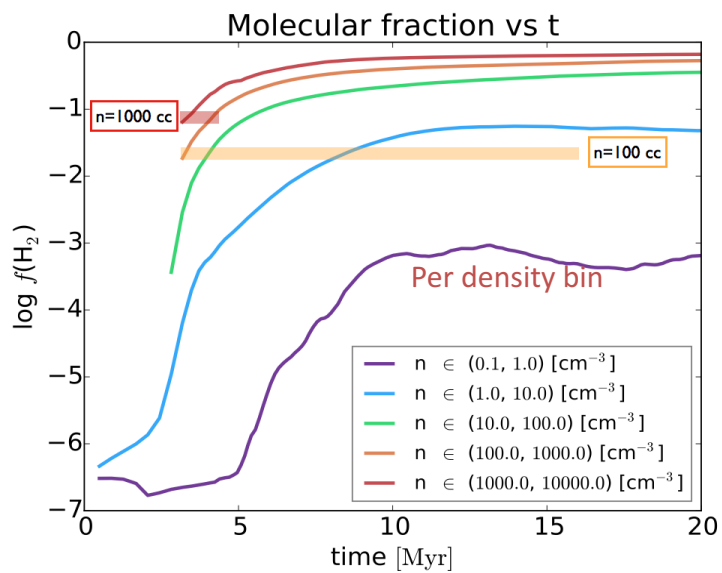
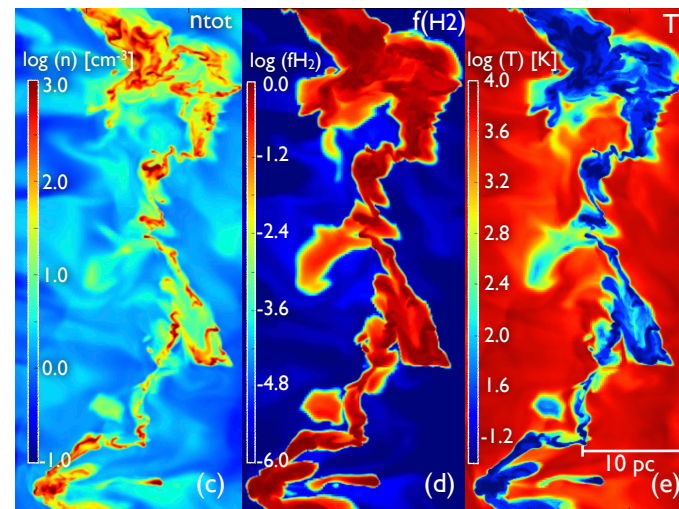
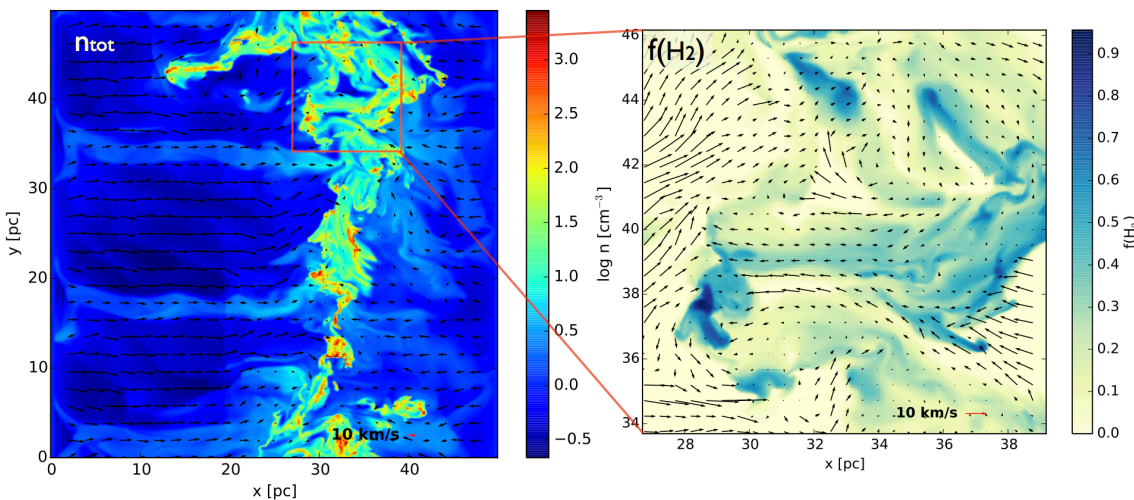
Timescales required to reach the equilibrium abundance.

$t(H_2) > t_{species}$  &  $dt > t_{species}$   
 $n > 3 \text{ cm}^{-3}$  or  $f_{sh,H_2} < 10^{-2}$



Mass distribution in the simulation  
 2D PDF:  $f_{sh,H_2}$  vs density

# Numerical Simulation: Results On H<sub>2</sub>



(Valdivia et al. 2016)

# Post-processing:

Compute equilibrium abundances  $(n, T, A_V, f_{\text{sh,H}_2}, B)$

## Out-of-equilibrium H<sub>2</sub>:

Non-equilibrium H<sub>2</sub> from simulation

## H<sub>2</sub> at equilibrium:

Abundances at equilibrium for all the species including H<sub>2</sub> and HI  
( $n, T$ , and shielding from simulation)

## With ion-neutral drift:

Non-equilibrium H<sub>2</sub>

Iterative method

- $v_d \approx \frac{(\nabla \times \mathbf{B}) \times \mathbf{B}}{4\pi \sum_{jk} n_j n_k \mu_{jk} K_{jk}}$
- $T_{\text{eff}} = T_{\text{gas}} + \Delta T$
- $\Delta T = \frac{\mu}{3k} v_d^2$
- $k \propto \exp(-\max\{\frac{\beta}{T_{\text{eff}}}, (\beta - 3\Delta T)/T\})$

## Without ion-neutral drift:

Non-equilibrium H<sub>2</sub>

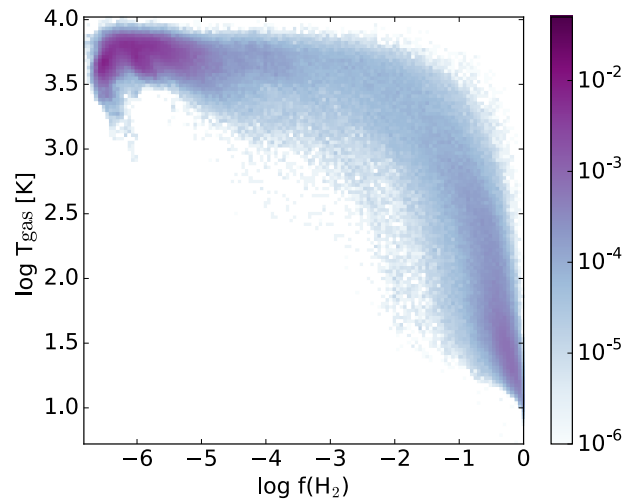
$$v_d = 0$$

$$T_{\text{gas}}$$

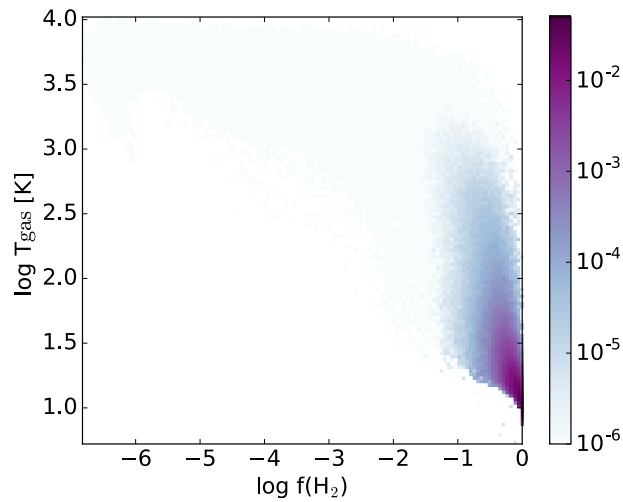


# Role Of Warm H<sub>2</sub>: 2D PDF

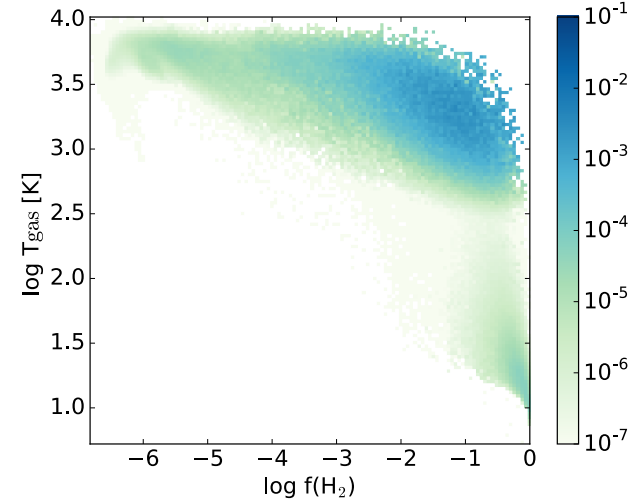
Volume



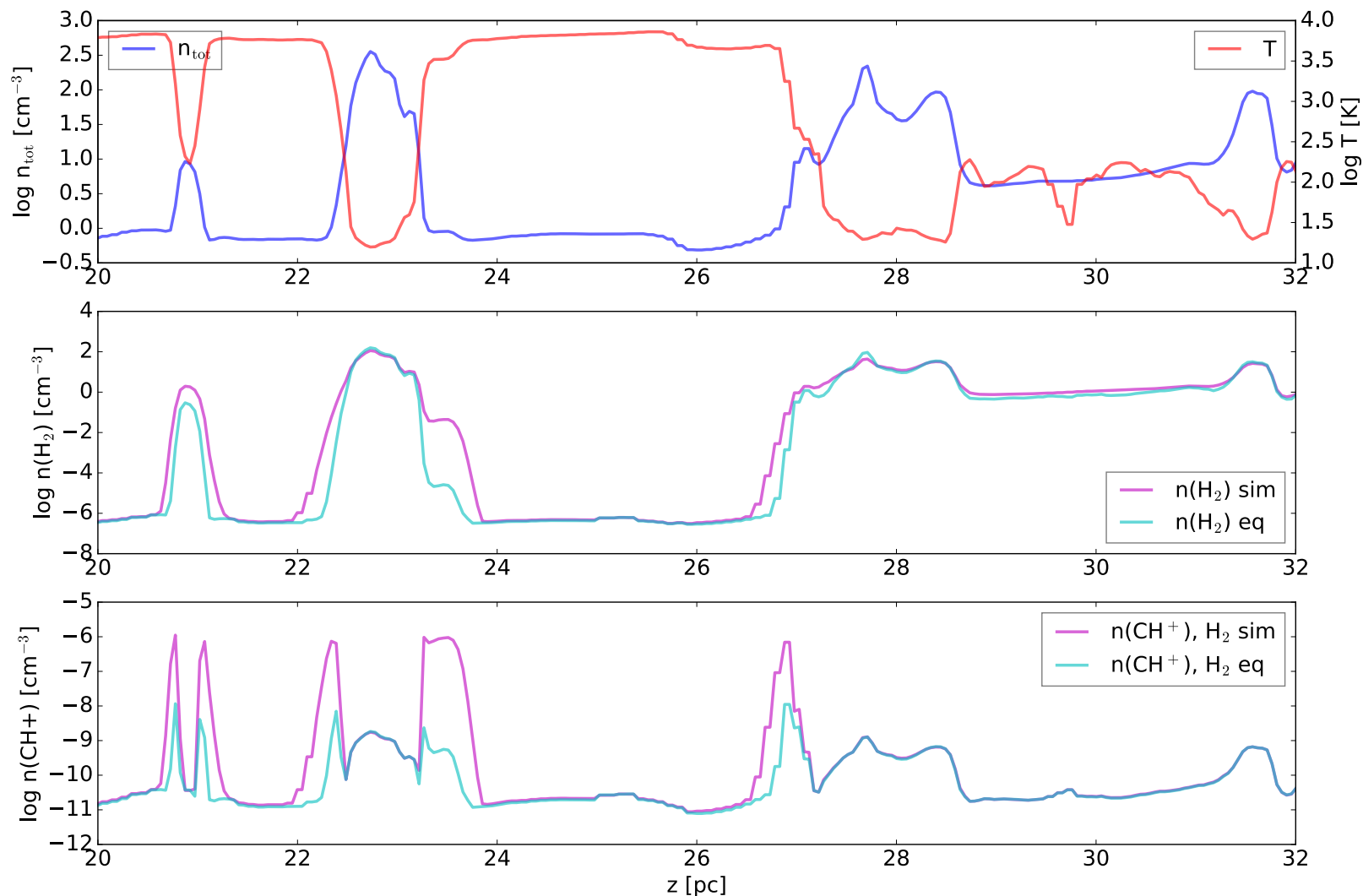
m(H<sub>2</sub>)



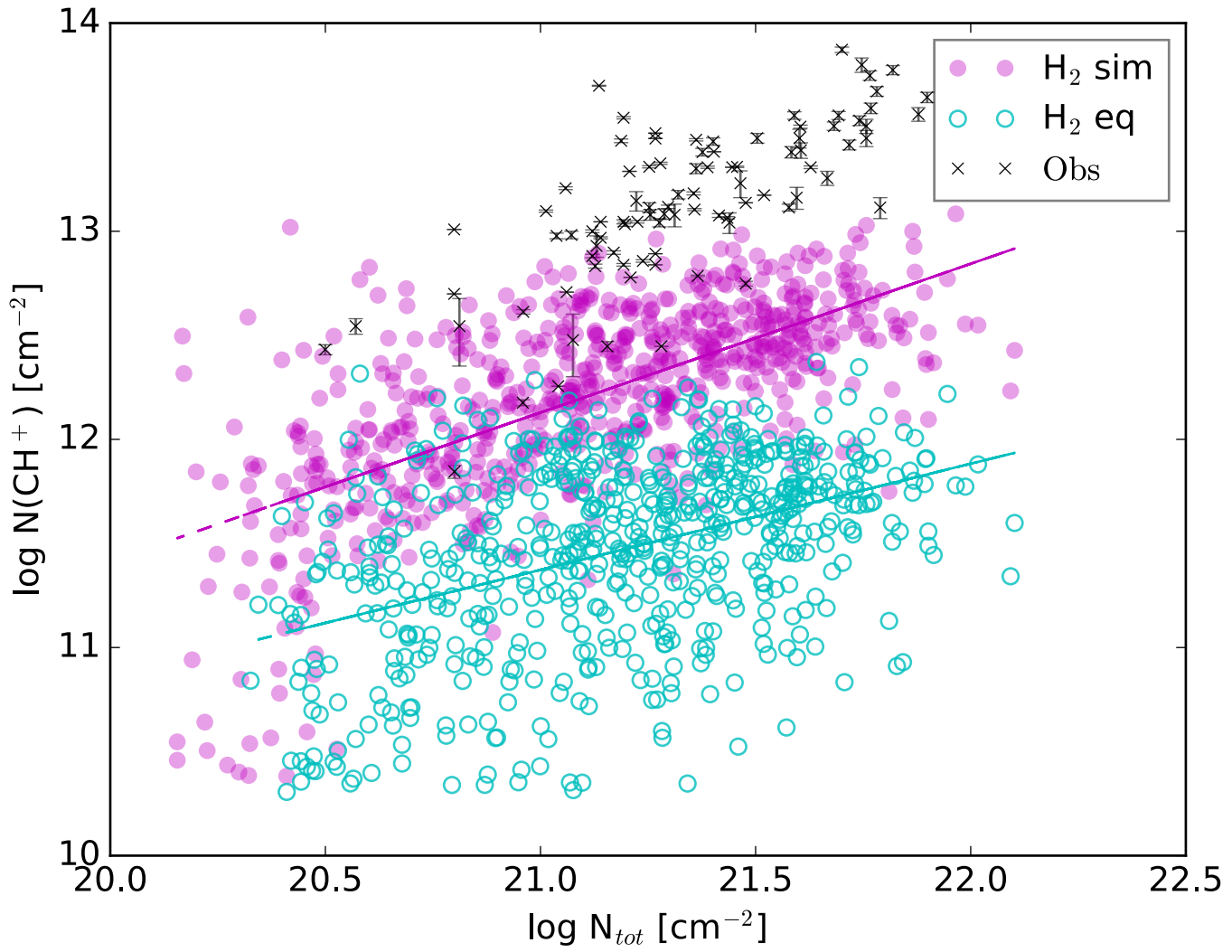
CH<sup>+</sup>



# Role Of Warm H<sub>2</sub>: LOS Analysis



# Role Of Warm H<sub>2</sub>: N(CH<sup>+</sup>) vs N<sub>tot</sub>



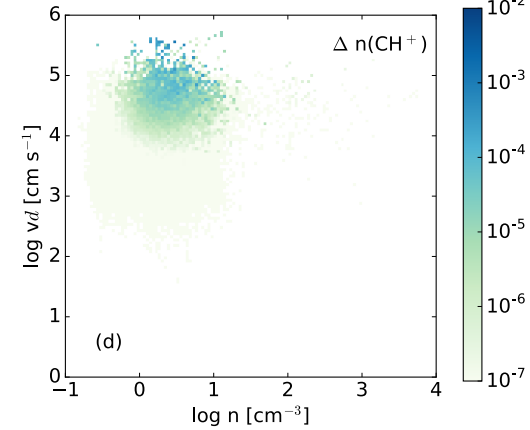
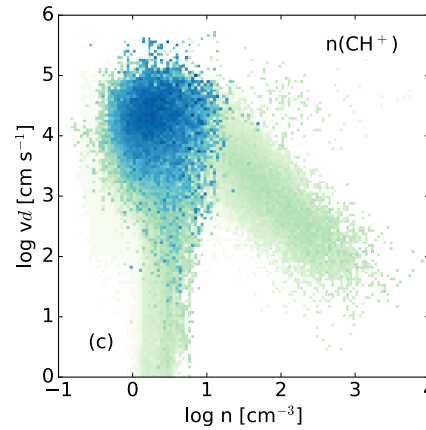
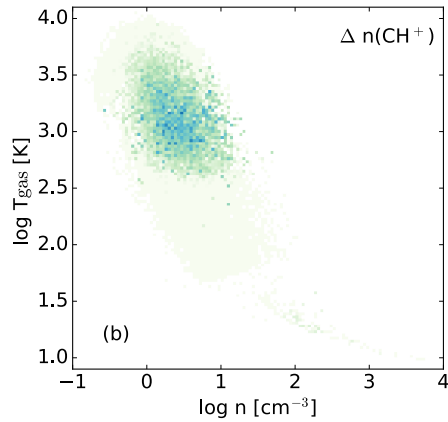
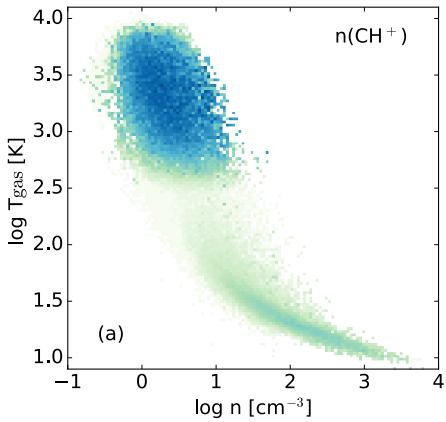
# Role Of The Ion-Neutral Drift: 2D PDF

$$T_{\text{eff}} = T_{\text{gas}} + \Delta T$$

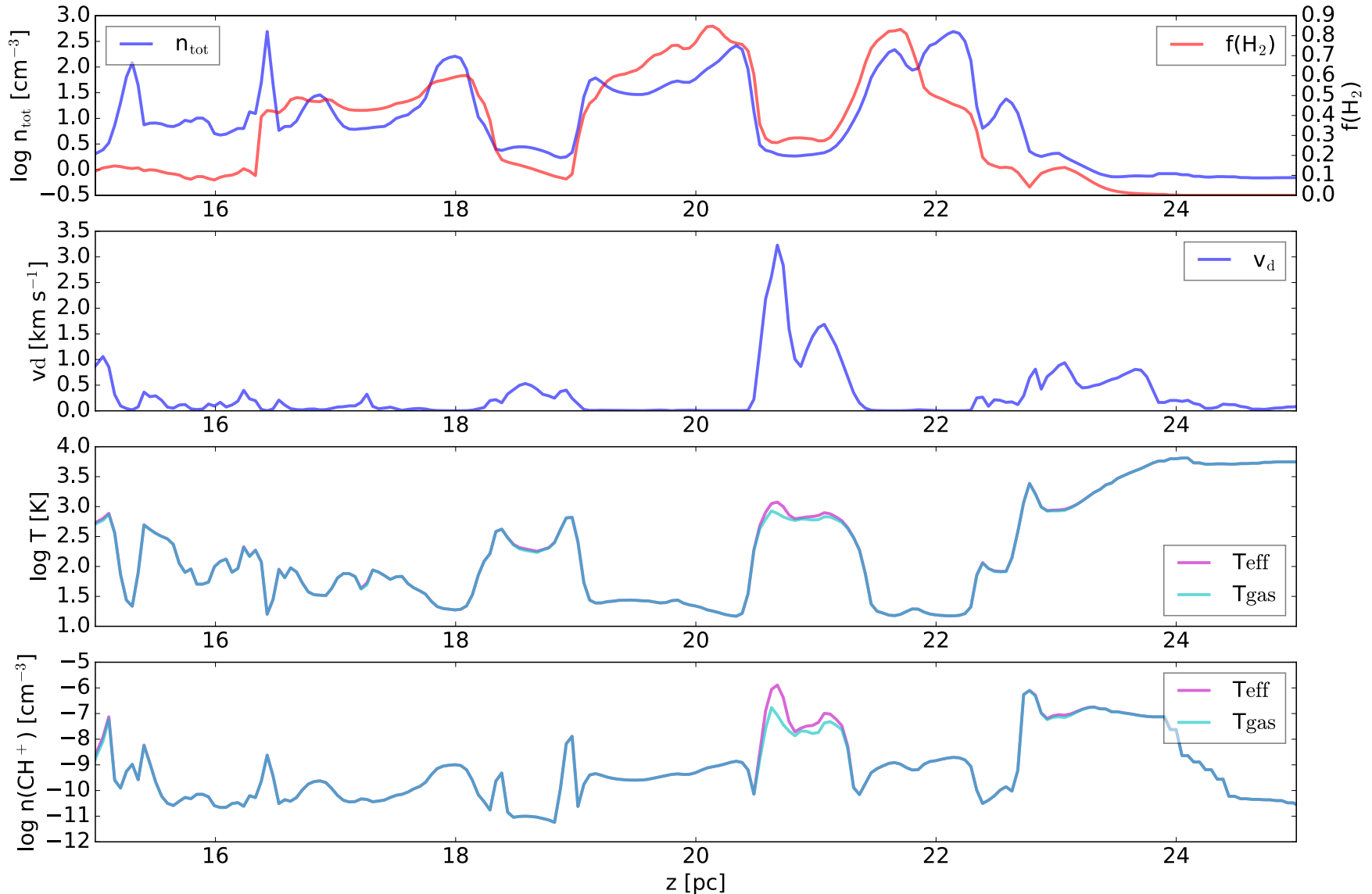
Residual

$$T_{\text{eff}} = T_{\text{gas}} + \Delta T$$

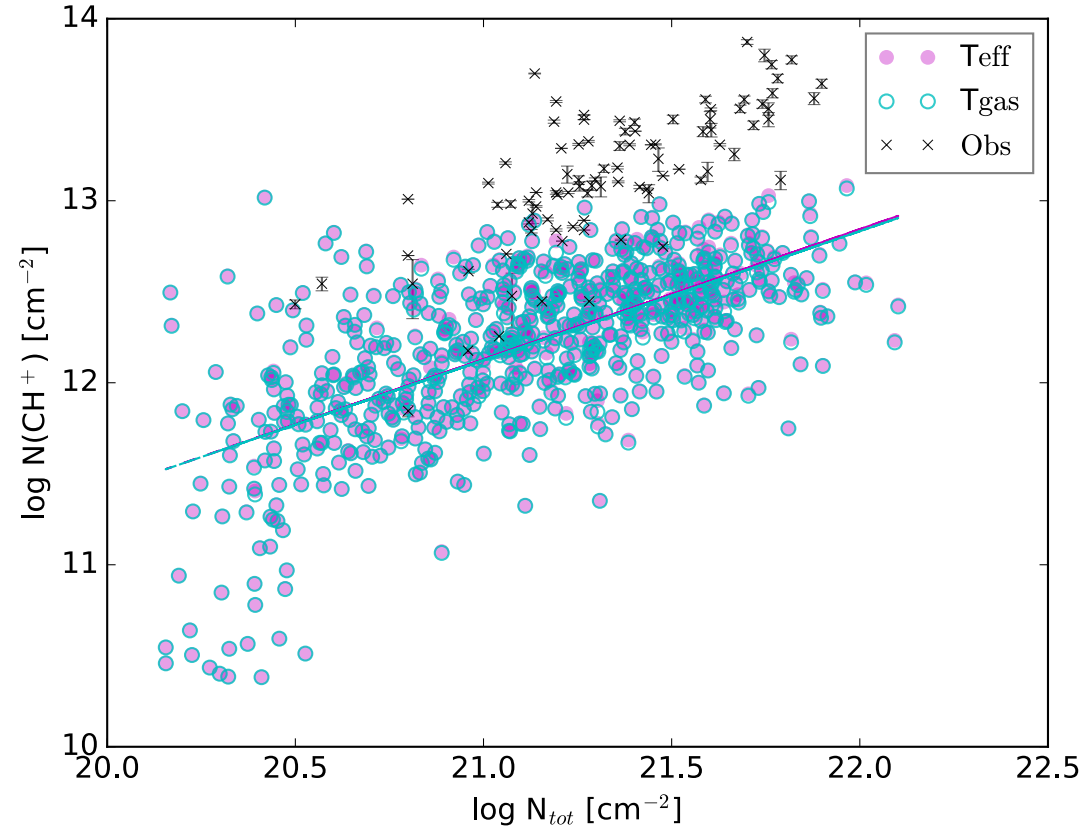
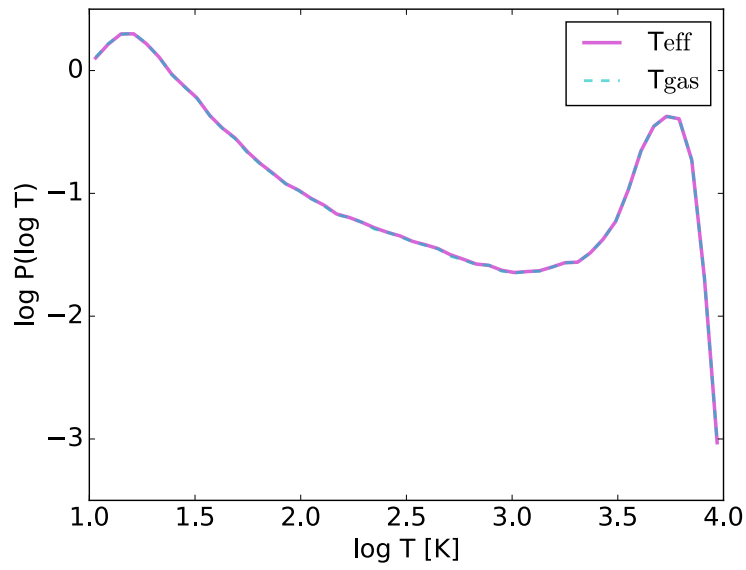
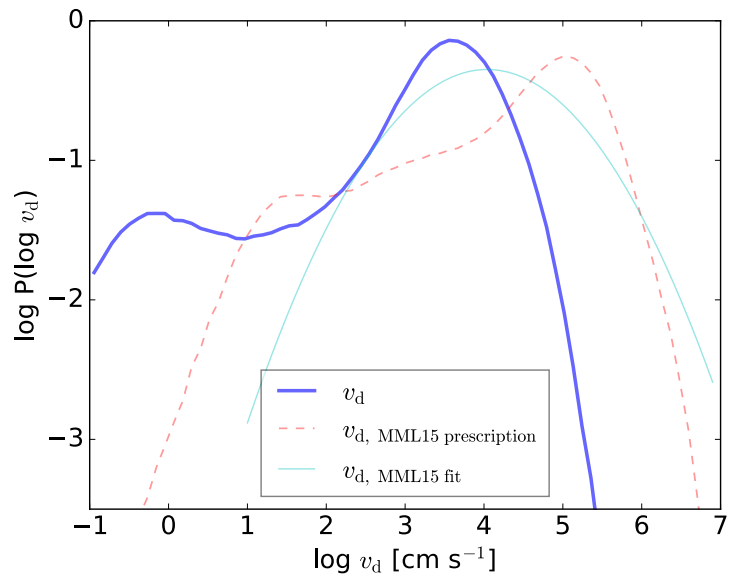
Residual



# Role Of The Ion-Neutral Drift: LOS Analysis

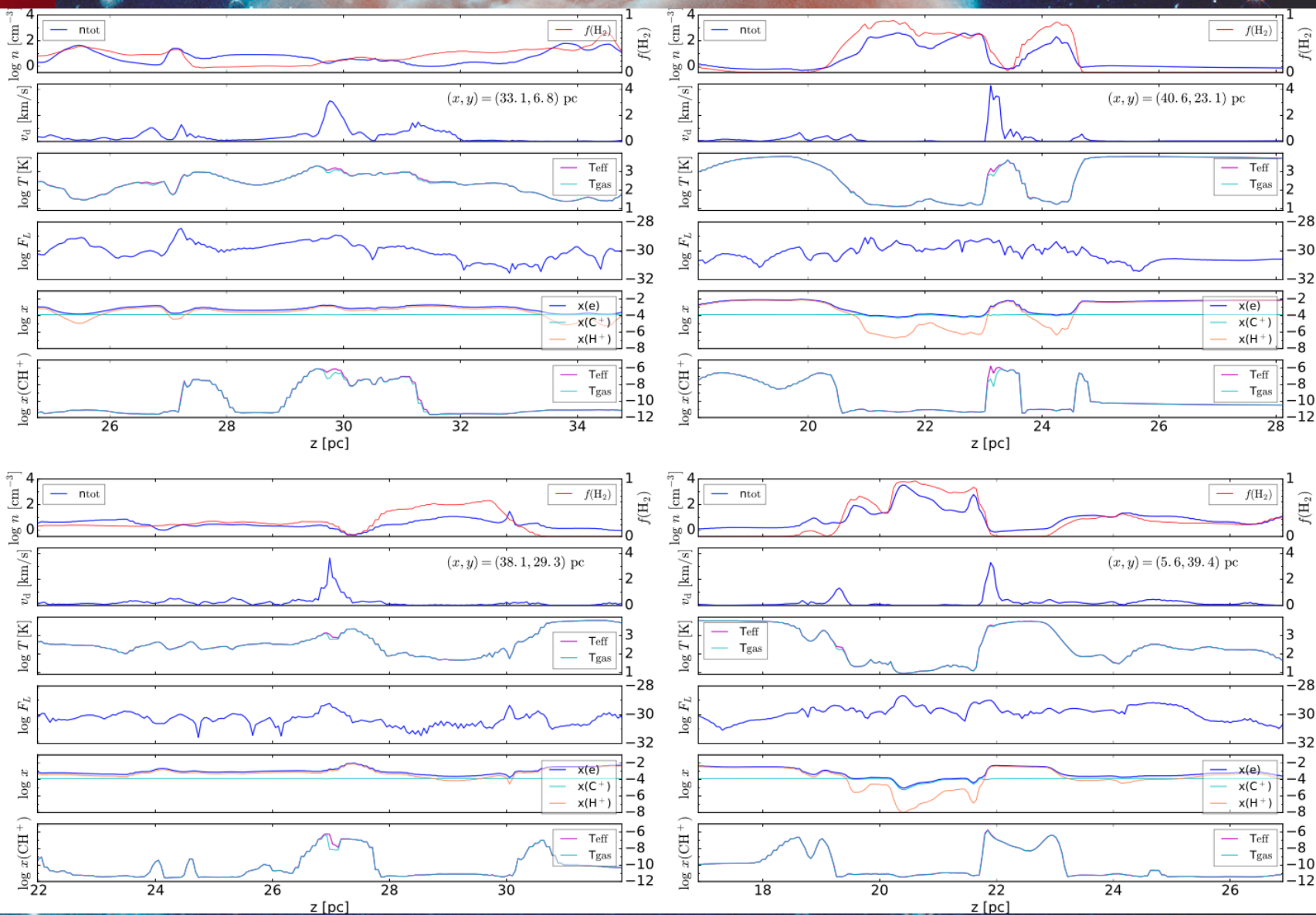


# Role Of The Ion-Neutral Drift: $N(\text{CH}^+)$ vs $N_{\text{tot}}$



- $v_d \propto \frac{1}{\rho_i \rho_n}$

# Role Of The Ion-Neutral Drift: LOS Analysis

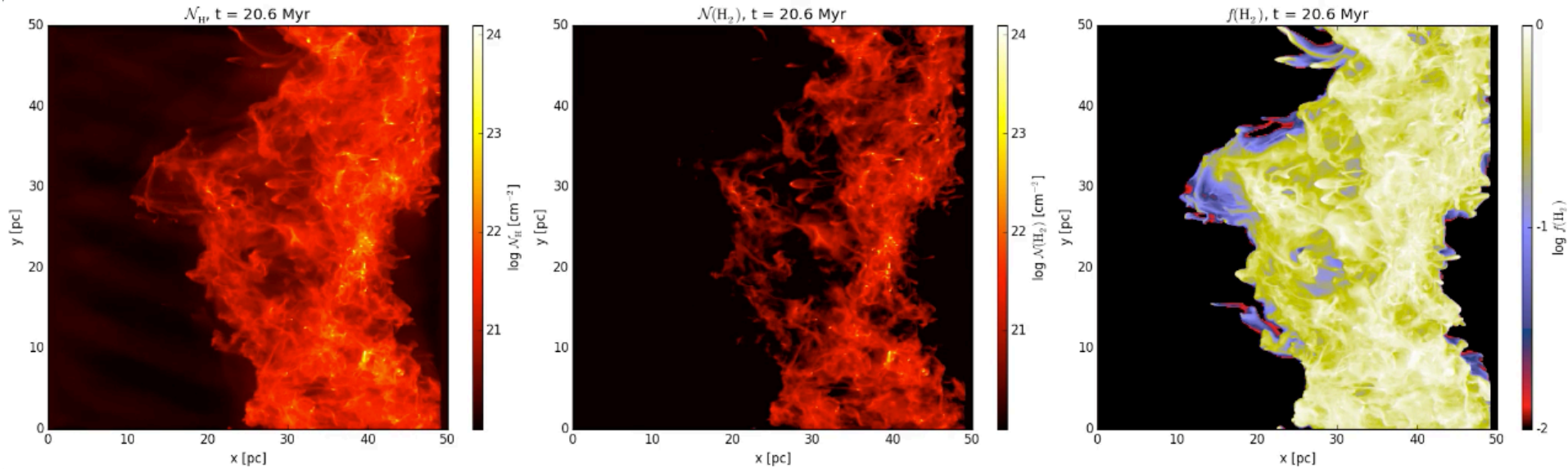


- It is possible to make a **hybrid approach** to include the **dynamical effects** on the most sensitive species (those with long evolution times) at a reasonable computational cost: species that react fast can be calculated at equilibrium with respect to the «dynamically» calculated species.
- **Warm H<sub>2</sub>** is crucial to efficiently form CH<sup>+</sup>, nevertheless the abundances of CH<sup>+</sup> are **still underpredicted** compared to observations ([Crane et al. 1995](#); [Gredel 1997](#); [Weselak et al. 2008](#))
- The formation of CH<sup>+</sup> seems to be more efficient in **regions where H<sub>2</sub> is not expected at equilibrium**.
- **High ion-neutral drift velocities** can boost the CH<sup>+</sup> formation, but these events are **extremely rare** => The effect is **negligible**.
- A good description of **small-scale physics** is necessary to avoid unrealistic v<sub>d</sub> distributions.
- **Possible clues:** dissipation of turbulence ([Falgarone et al. 2010](#), [Godard et al. 2009, 2014](#)), UV pumped H<sub>2</sub> levels ([Zanchet et al. 2013](#); [Herráez-Aguilar et al. 2014](#))





# Ideal MHD multiphase simulation



RAMSES AMR code  
(Teyssier 2002)

$$L = 50 \text{ pc}$$

$$N = 1 \text{ cm}^{-3}$$

$$V_{\text{in}} = 15 \text{ km s}^{-1}$$

$$B = 2.5 \text{ } \mu\text{G}$$

$$dx_{\text{min}} = 0.05 \text{ pc}$$

$$dx_{\text{max}} = 0.2 \text{ pc}$$

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) = 0,$$

$$\frac{\partial \rho \mathbf{v}}{\partial t} + \nabla \cdot (\rho \mathbf{v} \mathbf{v} - \mathbf{B} \mathbf{B}) + \nabla P = -\rho \nabla \phi,$$

$$\frac{\partial E}{\partial t} + \nabla \cdot [(E + P) \mathbf{v} - \mathbf{B}(\mathbf{B} \mathbf{v})] = -\rho \mathcal{L},$$

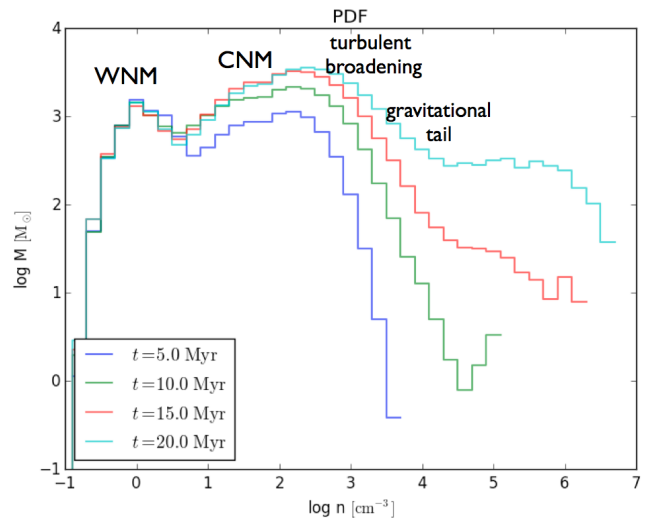
$$\frac{\partial \mathbf{B}}{\partial t} + \nabla \cdot (\mathbf{v} \mathbf{B} - \mathbf{B} \mathbf{v}) = 0,$$

$$\nabla^2 \phi = 4\pi G \rho,$$

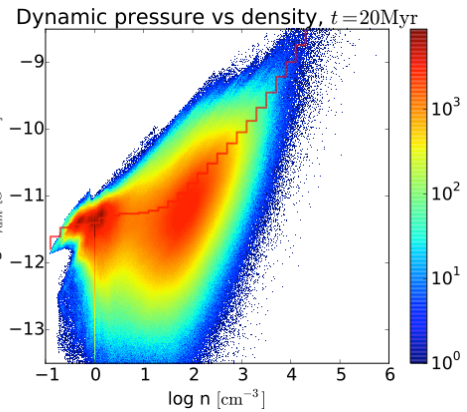
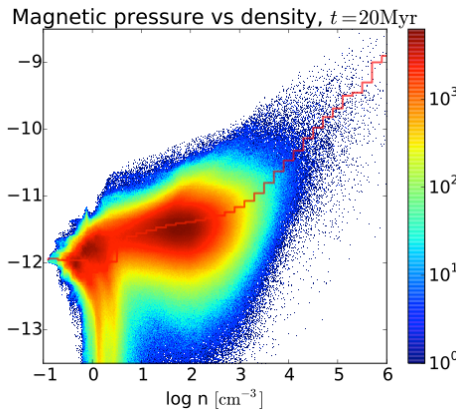
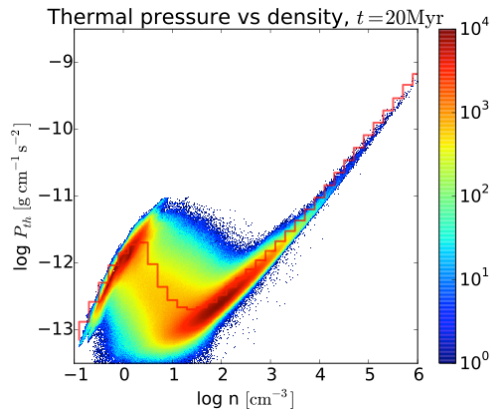
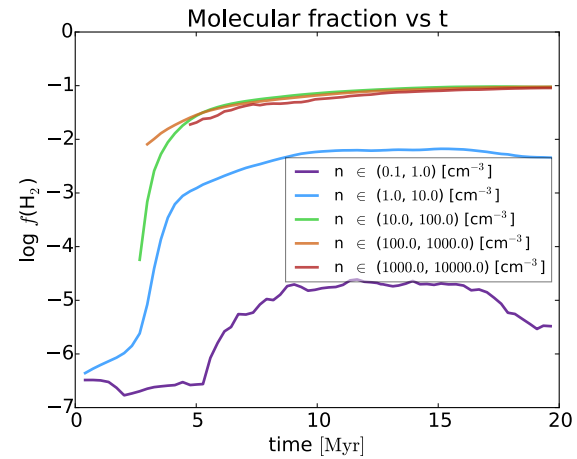
(Valdivia et al. 2016)

$$\frac{\partial n_{\text{H}_2}}{\partial t} + \nabla \cdot (n_{\text{H}_2} \mathbf{v}) = k_{\text{form}} n(n - 2n_{\text{H}_2}) - k_{\text{ph}} n_{\text{H}_2}$$

# Origin of warm H<sub>2</sub>



H<sub>2</sub> formation suppressed for  $n_{\text{thresh}} \geq 100 \text{ cm}^{-3}$

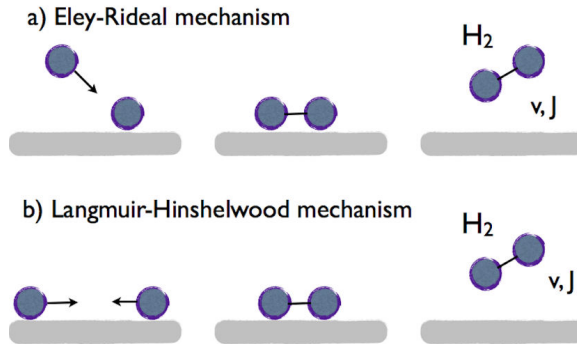
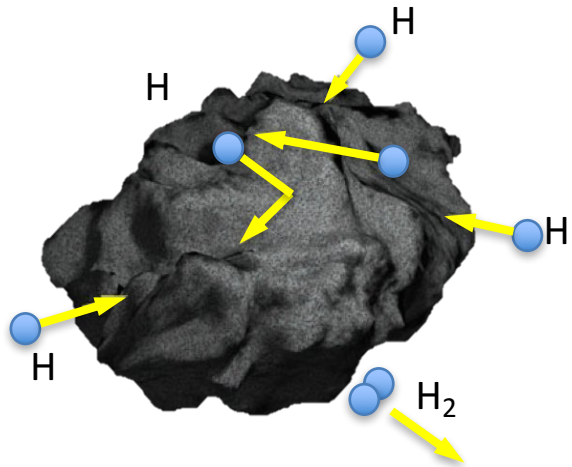


- Clumps are dominated by the **turbulent pressure** => **Transient** structures
- H<sub>2</sub> can be **transported** from cold and dense regions towards **warm and diluted** environments, where it survives due to the shielding provided by the **multiphase structure**

(Valdivia et al. 2016)

# H<sub>2</sub> formation

## H<sub>2</sub> formation on grain surfaces



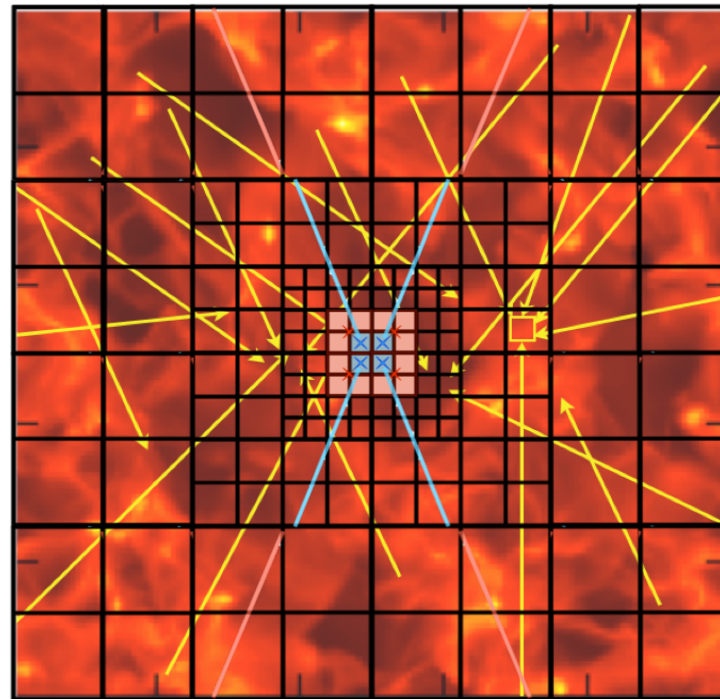
$$k_{\text{form}} = \underbrace{3 \times 10^{-17}}_{k_0 \text{ (Jura 1974)}} \times \sqrt{\frac{T}{100 \text{ K}}} \times \underbrace{\frac{1}{1 + \left(\frac{T}{464 \text{ K}}\right)^{1.5}}}_{\text{Sticking factor (Le Bourlot et al. 2012, Bron et al. 2014)}} \text{ cm}^3 \text{ s}^{-1}$$

# H<sub>2</sub> destruction

H<sub>2</sub> destruction by UV fluorescent photodissociation

$$k_{\text{ph}} = 3.3 \times 10^{-11} \times G_0 \underbrace{\langle e^{-\sigma_d \mathcal{N}} \rangle}_{\text{Dust shielding}} \times \underbrace{\langle f_{\text{shield}}(\mathcal{N}_{\text{H}_2}) \rangle}_{\text{Self-shielding (Draine \& Bertoldi 1996)}} \text{ s}^{-1}$$

UV photons

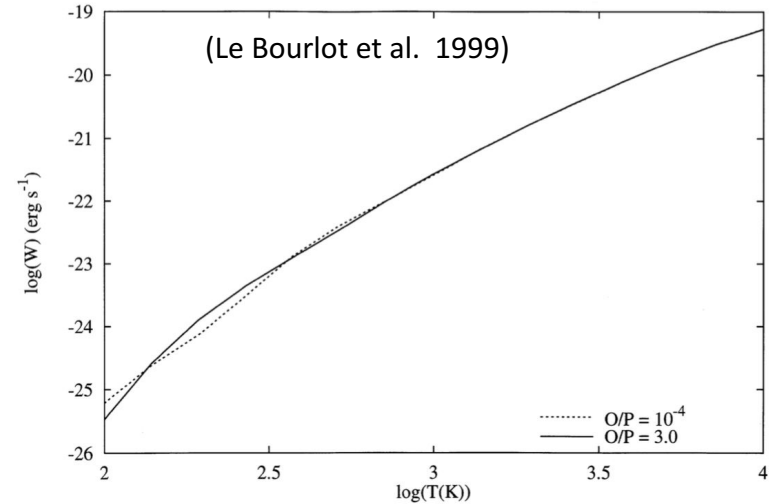


Tree-based method (Valdivia & Hennebelle, 2014)

## Cooling:

- H<sub>2</sub> line emission: (Le Bourlot et al. 1999)

$$W(\text{H}_2) = \frac{1}{n(\text{H}_2)} \sum_{vJ, v'J'} (E_{vJ} - E_{v'J'}) n_{vJ} A(vJ \rightarrow v'J')$$



## Heating:

- H<sub>2</sub> formation: 1.5 eV
- H<sub>2</sub> destruction: 0.4 eV (Black & Dalgarno 1977, Glover & Mac Low 2007)